TAVOLA DEGLI SVILUPPI DI TAYLOR DELLE FUNZIONI ELEMENTARI PER $x \to 0$.

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\begin{aligned}
e^x &= 1 + x + \frac{x^2}{2} + \frac{x^3}{6} + \cdots + \frac{x^n}{n!} + o(x^n) \\
\sin x &= x - \frac{x^3}{6} + \frac{x^5}{5!} + \cdots + \frac{(-1)^n}{(2n+1)!}x^{2n+1} + o(x^{2n+2}) \\
\cos x &= 1 - \frac{x^2}{2} + \frac{x^4}{4!} + \cdots + \frac{(-1)^n}{(2n)!}x^{2n} + o(x^{2n+1}) \\
\tan x &= x + \frac{x^3}{3} + \frac{2}{15}x^5 + \frac{17}{315}x^7 + \frac{62}{2835}x^9 + o(x^{10}) \\
\sinh x &= x + \frac{x^3}{6} + \frac{x^5}{5!} + \cdots + \frac{x^{2n+1}}{(2n+1)!} + o(x^{2n+2}) \\
\cosh x &= 1 + \frac{x^2}{2} + \frac{x^4}{4!} + \cdots + \frac{x^{2n}}{(2n)!} + o(x^{2n+1}) \\
\tanh x &= x - \frac{x^3}{3} + \frac{2}{15}x^5 - \frac{17}{315}x^7 + \frac{62}{2835}x^9 + o(x^{10}) \\
\frac{1}{1-x} &= 1 + x + x^2 + x^3 + \cdots + x^n + o(x^n) \\
\log(1+x) &= x - \frac{x^2}{2} + \frac{x^3}{3} + \cdots + \frac{(-1)^{n+1}}{n}x^n + o(x^n) \\
\arctan x &= x - \frac{x^3}{3} + \frac{x^5}{5} + \cdots + \frac{(-1)^n}{2n+1}x^{2n+1} + o(x^{2n+2}) \\
\operatorname{arctanh} x &= x + \frac{x^3}{3} + \frac{x^5}{5} + \cdots + \frac{x^{2n+1}}{2n+1} + o(x^{2n+2}) \\
(1+x)^\alpha &= 1 + \alpha x + \frac{\alpha(\alpha-1)}{2}x^2 + \frac{\alpha(\alpha-1)(\alpha-2)}{6}x^3 + \cdots + \binom{\alpha}{n}x^n + o(x^n)
\end{aligned}
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$$\binom{\alpha}{n} = \frac{\alpha(\alpha-1)(\alpha-2)\cdot\cdots\cdot(\alpha-n+1)}{n!}$$

$$\sqrt{1+x} = 1 + \frac{x}{2} - \frac{x^2}{8} + \frac{x^3}{16} - \frac{5}{128}x^4 + \frac{7}{256}x^5 + o(x^5)$$

$$\arcsin(x) = x + \frac{x^3}{6} + \frac{3}{40}x^5 + o(x^5)$$

$$\arccos(x) = \frac{\pi}{2} - x - \frac{x^3}{6} - \frac{3}{40}x^5 + o(x^5)$$